



PRE-ANALYSIS OF PROPOSED
GEODETIC NETWORK
AT
BALL MOUNTAIN DAM
JAMAICA, VERMONT

U.S. Army Corps of Engineers
New England Division

May 20, 1986

Submitted to

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New England Division
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by

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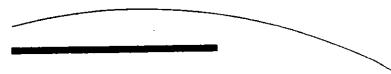
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The BSC Group



PREANALYSIS
OF
PROPOSED
GEODETIC NETWORK
AT
BALL MOUNTAIN DAM
VERMONT
MAY 1986

450 Summer Street
Boston MA
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The BSC Group

May 20, 1986

617 350 4090

Mr. Stephen L. Whiteside, P.E.
Geotechnical Engineers, Inc.
1017 Main Street
Winchester, MA 01890

RE: Preanalysis of Proposed Geodetic Network
Ball Mountain Dam, VT

Dear Steve:

I am pleased to submit the attached report in connection with the above-referenced project.

The results outlined in the report indicate that required accuracy can be achieved.

Sincerely

THE BSC GROUP
Boston Survey Consultants

Kevin Hanley
Kevin Hanley, P.L.S.
Division Manager

Engineers

Surveyors

Scientists KH/gh

Architects

Landscape
Architects

Planners

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EXECUTIVE SUMMARY

In accordance with our contract with Geotechnical Engineers Inc., Winchester, Massachusetts, Boston Survey Consultants (BSC) has prepared this pre-analysis of the Proposed Monitoring Surveys for the Ball Mountain Dam, Vermont.

The nature of the dam and the natural topography is such that the implementation of a classical geodetic framework is not possible. Thus additional observations points must be included in the geodetic network to:

- (a) strengthen the framework and
- (b) ensure adherence to the accuracy requirements

The report prepared by Dr. Adam Chrzanowski in conjunction with Mark Rohde at the University of New Brunswick indicates that the level of accuracy required can be attained using the instrumentation and targetting proposed by BSC. As with any precision measurement survey extreme care is required. The design of the measurement approach is addressed in Section 4 and recommendations as to observing methodology have been suggested in order to attain the required accuracy.

REPORT

PRE-ANALYSIS OF PROPOSED MONITORING SURVEYS FOR THE BALL MOUNTAIN DAM ON THE WEST RIVER, VERMONT

Prepared for The BSC Group by
Dr. A. Chrzanowski, P.Eng., J. Secord and M. Rohde

1. INTRODUCTION

According to the letter of 25 November 1985, the following scope of services was requested:

1. Review topographic plans and photographs of the project site in order to determine preliminary location of the geodetic network. In addition, if deemed necessary, a site visit should be undertaken.
2. Perform a pre-analysis of the network to determine changes required in the network design to meet required accuracies, to predict probable accuracies based on the proposed instrumentation and to develop an observational methodology to achieve the required accuracies.

The topographic plans and photographs were supplied by Mr. Mark Rohde who had already visited the site under the employment of BSC in August 1985. Although a visit by these consultants was deemed necessary, the time constraint imposed by BSC for the results of the pre-analysis to be delivered by 29 November 1985 required that only the immediately available information could be utilized. The information consisted of:

- i) Photographs of the dam and its environs;
- ii) Proposed geodetic network overlayed on a Corps of Engineer's General Plan of the dam at a scale 1" = 100'; ..

- iii) Proposed layout of instrumentation at a scale 1" = 50';
- iv) Survey instrumentation to be used which consists of:
 - Wild T3 or T2000 theodolites,
 - Wild DI4L EODM instrument,
 - Wild traversing targets,
- v) Verbal information on the proposed monumentation which would allow (in most cases) for self-centering of the instruments and targets ;
- vi) Verbal communication that the expected movement of the dam would be 3 mm per month.

2. APPROACH TO THE PRE-ANALYSIS

The pre-analysis for deformation surveys requires greater computational effort and more sophisticated procedures than for conventional geodetic surveying.

Over the past five years a generalized method (called the UNB Generalized Method) for the analysis of deformation surveys has been developed in the Department of Surveying Engineering at the University of New Brunswick which allows a versatile treatment of such surveys with possible integration of any type of observables, not only geodetic but also geotechnical, such as tilt, strain and other physical measurements. This method is described in Appendices 4 and 5, and has been applied in several geotechnical projects such as: monitoring of dyke deformations in oil fields in Venezuela, dam deformation studies at Mactaquac, N.B., tectonic deformations in Peru and ground subsidence studies in coal mining areas in Western Canada to name only a few. The generalized approach allows determining not only single point displacements but also more general deformation parameters such as strain components and relative rigid body motion. In this particular application in the pre-analysis for monitoring the deformation of the Ball Mountain Dam, only the detection of single point displacements on the dam structure and in the reference network was

considered. One should emphasize that in deformation studies a treatment of reference points as fixed and errorless is incorrect, particularly in the case of the Ball Mountain Dam where the aperture of the reference network is small, about 400 m, and the points are close to the reservoir.

The changeable water level of the reservoir may induce ground movements to a considerable distance from the dam structure. In addition, the possible local movement of the survey monuments (frost action, thermal deformations, etc.) cannot be ignored. Therefore, in the UNB Generalized Method, after at least two campaigns of survey, the detection of unstable points in the reference network is done first through a trend analysis and later in the overall analysis the unstable reference points are treated as additional object points. In the course of pre-analysis one cannot predict which of the reference points may be unstable. Therefore, a provision must be made when designing the accuracy of the survey that the relative positions of the reference points must be determined with, at least, the same or better accuracy than is the tolerance for detecting the movements of the object points.

In the UNB Generalized Method, the modelling of movement is derived by least squares fitting of a selected displacement function to the displacement field incorporating all the points within the network and their associated variances and covariances. In turn, the displacement field results from the combination of two or more campaigns of observation. Pre-analysis and the designing for detection of movement follow the same path, from the observation field through the displacement field to the parameter space describing the movement. Algorithms for the analysis and design (pre-analysis) have been developed (Chen, 1983) and implemented in the Department (Secord, 1984) and were utilized in this design.

Since the displacement of 0.003 m in either the horizontal or the vertical direction is to be detected by monthly surveys, the pre-analysis has recognized a value of ± 0.003 m as a tolerance at the 0.95 level of confidence. This tolerance imposed the limit on the detection of displacement in x, y, or z between two campaigns. Hence, into a single campaign of horizontal survey (i.e. separating x, y movement), this tolerance becomes a standard deviation of

$$\frac{\pm 0.003}{2.4484\sqrt{2}} = \pm 0.0008 \text{ m}$$

and in the vertical (z movement only), the tolerance translates into a standard deviation of

$$\frac{\pm 0.003}{1.96\sqrt{2}} = \pm 0.0011 \text{ m}$$

for positioning in a single campaign.

After examination of the above material, the consultants decided that for the purposes of pre-analysis the geometry of the monitoring network as proposed by BSC could be accepted without any major changes except for the relocation of one reference point (point P3 on the attached plan of the network) from which the targets on the dam structure should be visible. Also one target point was added on the intake tower so that the stability of that structure should be included in the study. As far as the type of observables to be used in the monitoring surveys was concerned, direction measurements with the Wild T2000 have been favoured in the pre-analysis with only a few distances to be measured for the control of the scale of the reference network.

The pre-analysis of the vertical movements was based on the assumption that the vertical movements will be determined by trigonometric height traversing by measuring zenith angles to the targets on the dam and

between all reference points and by using distances and their variances derived from the adjusted coordinates obtained from the horizontal surveys.

Special attention has been paid to the influence of the possible changes in atmospheric refraction between the survey campaigns. The commonly accepted value of the coefficient of refraction $k = 0.13$ is valid only for the lines of sight passing above the ground surface at 40 metres or higher. In the first few metres above the ground the coefficient may reach the value of -10 or even more (Chrzanowski, 1985) with significant seasonal changes, which may be the case in the project area. For instance, if over an average distance of 200 m the value of k would change from 0 to -2 which is quite likely, the height difference determination would change by 6 mm.

3. RESULTS OF THE PRE-ANALYSIS

3.1 Pre-analysis of Horizontal Movements

A preliminary pre-analysis involved several variants on the types and number of observables to be used within the given geometry of the network. The finally accepted scheme is shown in Fig. 1 in which the 6 reference points and 28 object points (including the Tower target as an object point) are connected by 103 directions observed from reference stations: P1, P2, P3, P4, and P5 (only P6 being not occupied) and only 4 distances observed from station P4 as shown by heavy lines in Fig. 1. Apparently, preliminary pre-analysis has shown that the variants on the distribution (localization) of the few measured distances in the network did not alter significantly the result of the pre-analysis. The choice of having the deformation surveys relying mainly on direction measurements rather than distances was made on the basis of the available

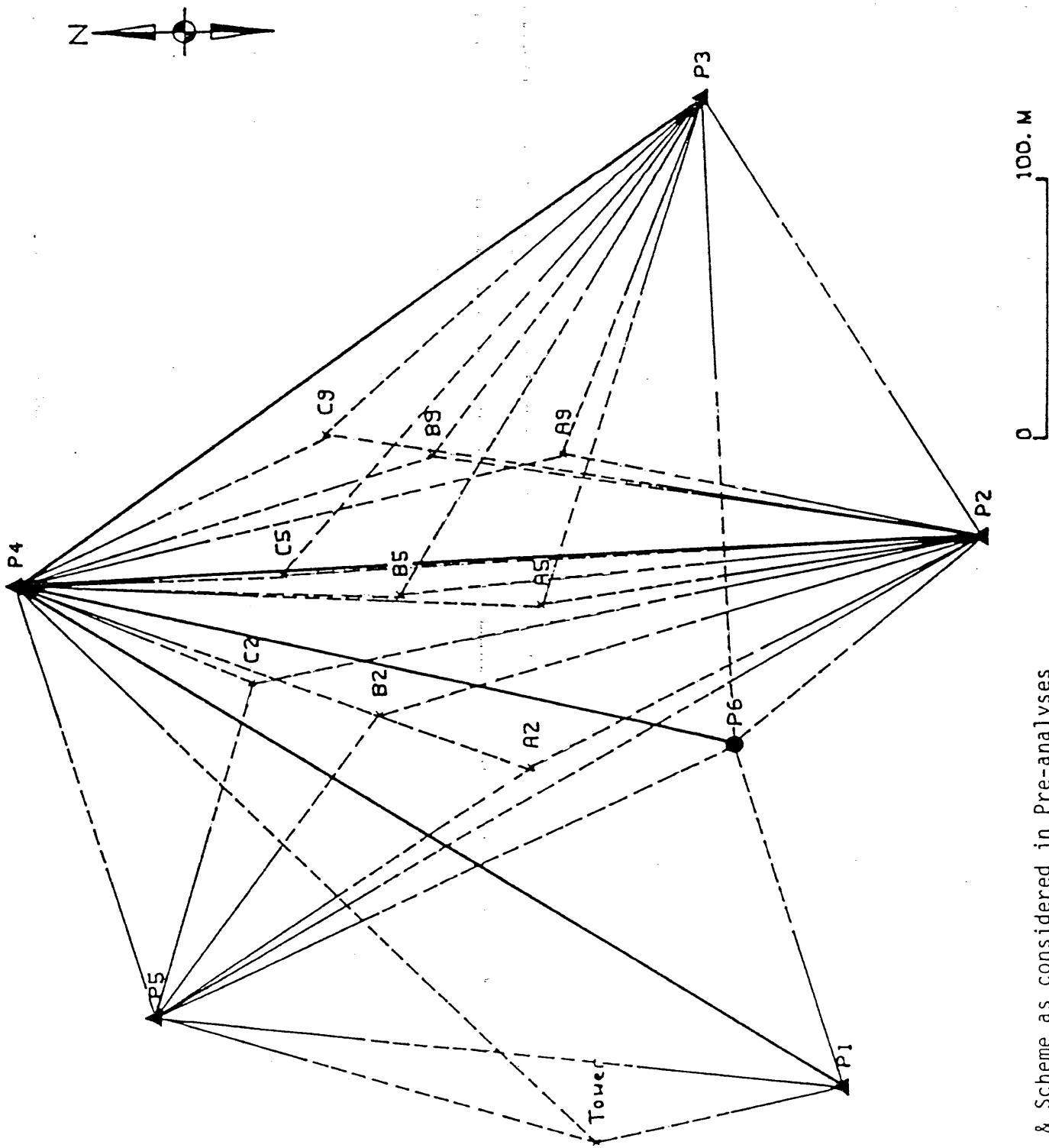


Figure 1 Network & Scheme as considered in Pre-analyses

instrumentation and their precision, topography and, connected with it, logistics in placing retroreflectors on too many points.

Due to the very limited time allowed for the pre-analysis, only 10 object points were included in the computations as representative of the likely result for all of the other points. The approximate coordinates (x , y , z) of all the analysed points were determined from the attached plan using a local x , y coordinate system and the contours.

The pre-analysis was done in the following steps using the UNB software for the Generalized Method:

- i) Determination of variances and covariances of coordinates of all the points through the propagation of accepted variances of observations holding one point and one direction in the network fixed and errorless (minimal constraints). One should emphasize that in the UNB Generalized Method the choice of the minimal constraints is irrelevant because the modelled movements are datum independent.
- ii) Determination of the relative error ellipses (all combinations) for a preliminary evaluation of the detectability of relative point movements.
- iii) Modelling of deformation, which in the case of single point movements is very simple; for each reference point the model is $dx_i = 0$ and $dy_i = 0$ with their appropriate variances and covariances and for the object points, $dx_i = a_i$ and $dy_i = b_i$ where a and b are to be determined through the least squares fitting of the model to the observed displacements. In the pre-analysis, only the variances and covariances of the a_i and b_i parameters are determined.
- iv) Depiction of the error ellipses corresponding to the variance and covariance of the a_i and b_i , for the displacements of the object points at the 0.95 confidence level and their comparison with the accepted tolerance (0.003 m in this project).

The final pre-analysis was made for the following 3 different accuracies of observations:

Analysis No. 1: direction measurements $\sigma = \pm 1''$

distance measurements $\sigma = \pm 5 \text{ mm} \pm 5 \text{ ppm}$

Analysis No. 2: direction measurements $\sigma = \pm 0.5''$

distance measurements $\sigma = \pm 5 \text{ mm} \pm 5 \text{ ppm}$

Analysis No. 3: direction measurements $\sigma = \pm 0.5''$

distance measurements $\sigma = \pm 3 \text{ mm} \pm 2 \text{ ppm}$

Results of steps i) and ii) above for the three variants of the pre-analysis are given in Appendices 1 to 3. The results of step iii) are shown in Table 1 and the final results, the error ellipses of the displacements with respect to the block of all the reference points, are shown in Figures 2 to 4.

The final results indicate that if the displacements would be expected to take place only in the down- and up-stream direction, the accuracies of the observations in Analysis No. 1 would be sufficient because the displacements of 3 mm would extend beyond the 95% error ellipses. However, if the detectability of the 3 mm movement would be required in all directions, then the accuracies of observations should be, at least, as accepted in Analysis No. 2 or even Analysis No. 3.

3.2 Pre-analysis of Vertical Movements

The pre-analysis followed the same steps as the analysis of the horizontal movements using approximate heights of the points as determined from the topographic plan. Of course, error ellipses do not apply to the unidimensional case. The same number of zenith angles as horizontal directions (observed simultaneously from the same stations) has been taken

Table 1. Standard Deviations of Single Point Rigid Body Displacement Components

Point	Standard deviation in x component (a_i)	Standard deviation in y component (b_i)
A2	+ 0.0011 m	+ 0.0021 m *
	- 0.0006	- 0.0010 **
	0.0006	0.0010 ***
A5	0.0010	0.0017
	0.0005	0.0008
	0.0005	0.0008
A9	0.0010	0.0012
	0.0005	0.0006
	0.0005	0.0006
B2	0.0009	0.0013
	0.0004	0.0006
	0.0004	0.0006
B5	0.0009	0.0020
	0.0005	0.0010
	0.0005	0.0010
B9	0.0011	0.0018
	0.0005	0.0009
	0.0005	0.0009
C2	0.0007	0.0009
	0.0004	0.0005
	0.0004	0.0005
C5	0.0008	0.0026
	0.0004	0.0013
	0.0004	0.0013
C9	0.0014	0.0025
	0.0007	0.0012
	0.0007	0.0022
Tower	0.0003	0.0011
	0.0003	0.0011
	0.0003	0.0011

* directions + 1.0" distances + 0.005 m + 5 ppm

** directions \pm 0.5" distances \pm 0.005 m \pm 5 ppm

*** directions \pm 0.5" distances \pm 0.003 m \pm 2 ppm

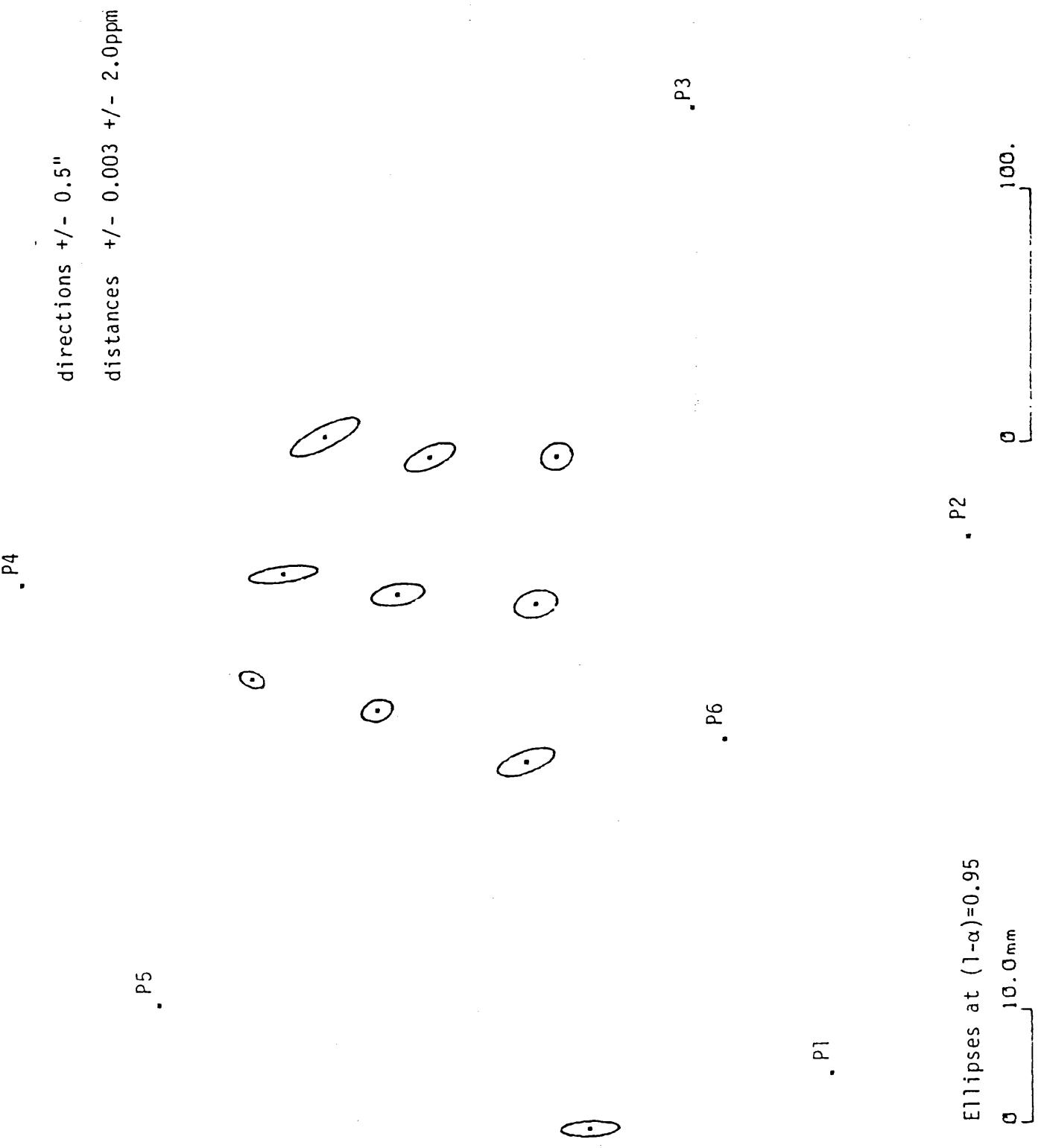
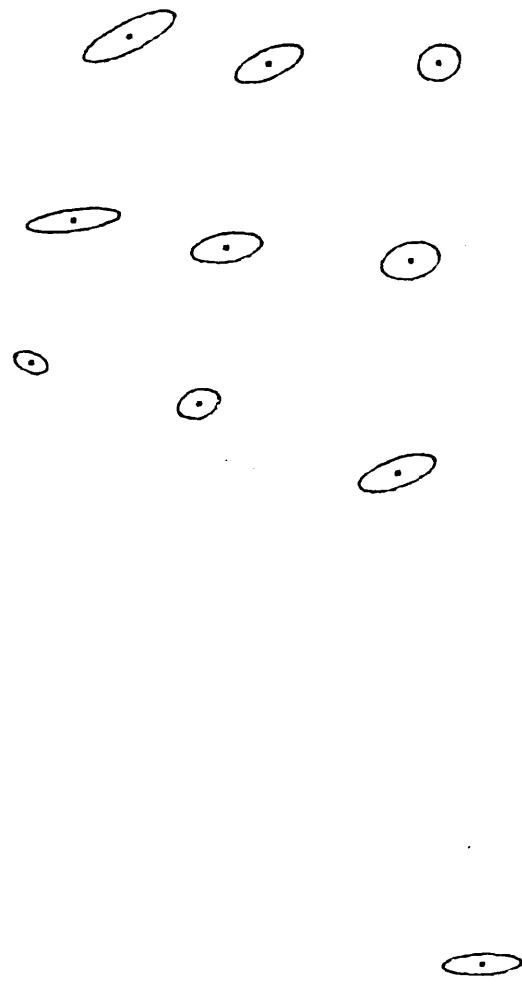


Figure 4 Analysis No. 3 Single Point Rigid Body Movement Error Ellipses

P4

directions +/- 0.5"
distances +/- 0.005 +/- 5.0 ppm



P5

-11-

P3

P6

P1

Ellipses at $(1-\alpha)=0.95$

0
10.0 mm
100.

P2

Figure 3 Analysis No. 2 Single Point Rigid Body Movement Error Ellipses

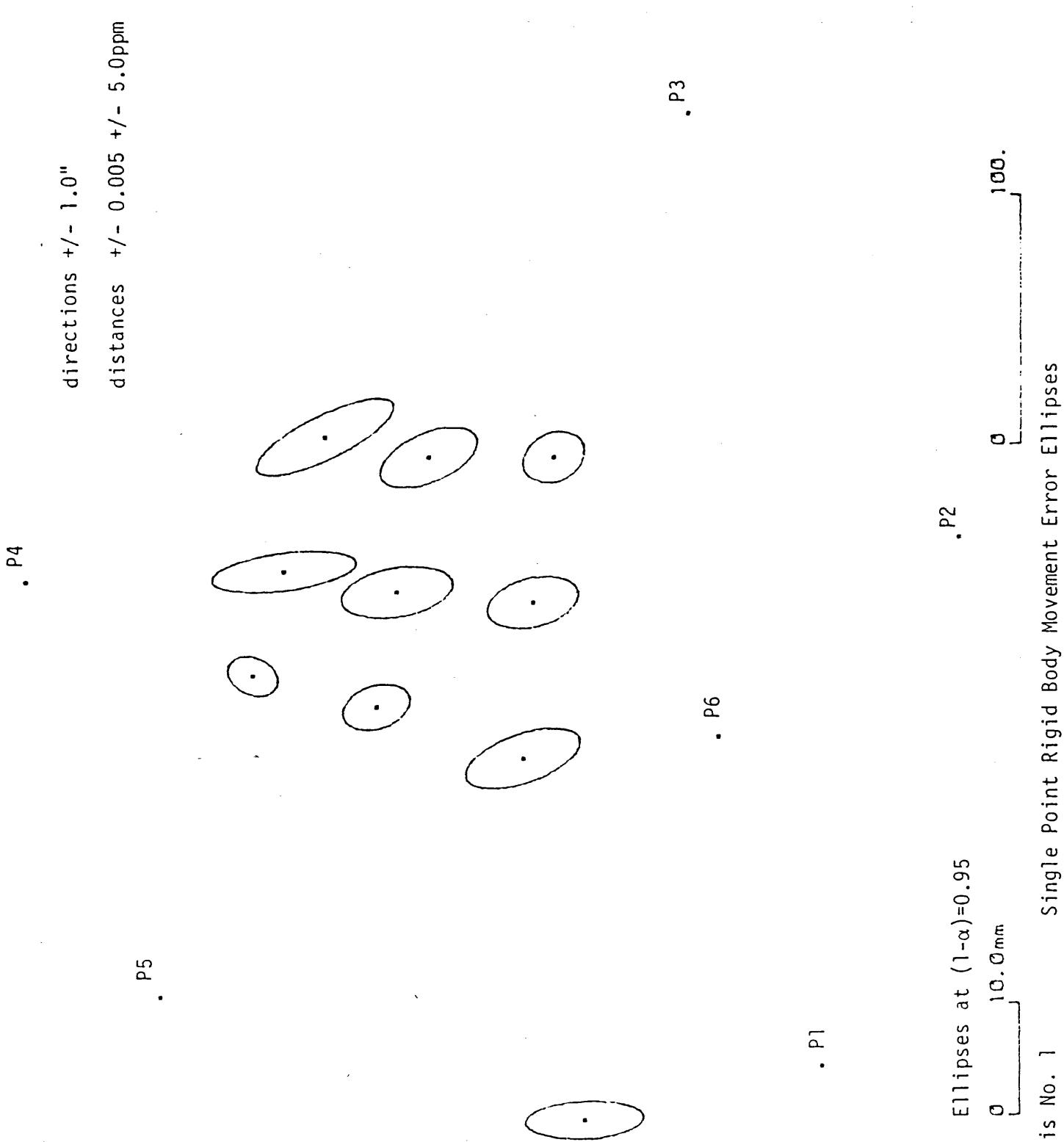


Figure 2 Analysis No. 1 Single Point Rigid Body Movement Error Ellipses

in the pre-analysis. Only one pre-analysis was made using $\sigma = 0.7''$ for zenith angles and distances derived from adjusted coordinates with variances and covariances as obtained from the pre-analysis of the horizontal network (analysis No. 2). In addition, errors of the coefficient of refraction were taken as $\sigma_k = \pm 0.5$ on those lines along which the terrain profile significantly goes downwards near the instrument station and $\sigma_k = \pm 1$ along other lines.

Table 2 lists the errors in vertical displacements at the 0.95 confidence level as obtained from the pre-analysis. As one can see the accuracies marginally meet the tolerance limit of 3 mm. It depends, of course, how well the atmospheric refraction will be known during the survey campaigns. Since this is difficult to predict, any additional pre-analysis with other accuracies of angle measurements would not be helpful. Some recommendations for controlling the effects of refraction are given in the next section.

4. DESIGN OF MEASUREMENTS

4.1 Horizontal Network

The design of measurements for detecting horizontal movements has been based on pre-analysis No. 2 which calls for directions to be measured with a standard deviation of $0.5''$ and distances with the standard deviation of $\pm 5 \text{ mm} \pm 5 \text{ ppm}$. These accuracies are achievable with the equipment available to the BSC Group, namely the electronic theodolite Wild T2000 and DI4L EODM instrument if certain conditions are satisfied.

Based on the extensive experience of these consultants (Chrzanowski, 1985) with the use of the T2000 and on the error analysis of pointing, reading, levelling and centering (Chrzanowski, 1984 and Chrzanowski, 1977), the accuracy of $0.5''$ is achievable if:

Table 2. Confidence Intervals at 0.95 for the Vertical Displacement Component

Point	Confidence Interval
Tower	0.99 mm
A2	2.91
A5	3.15
A9	3.06
B2	2.56
B5	3.00
B9	3.19
C2	2.28
C5	2.59
C9	3.02

- a) directions are measured in four sets (two positions of the telescope in each set);
- b) centering of the theodolite and of the targets (in the case of this project) is done with an accuracy better than 0.3 mm;
- c) levelling of the instrument, for measurements with inclination of lines up to 5^0 , with an accuracy better than 5" (achievable with a properly adjusted spirit level) and for inclinations up to 20^0 with an accuracy better than 1" which is achievable only when using the compensator of the vertical circle for levelling the instrument and when releveling the instruments between individual sets;
- d) using specially designed targets (Blachut et al., 1979);
- e) shading the instrument from direct solar radiation.

Since the measurements will be performed on pillars equipped with some kind of forced centering plates, point b) above should be easily satisfied with properly designed targets and their mountings. Since the BSC group decided to use Wild traversing targets, these consultants strongly recommend checking all the targets (at close range) for their centricity with respect to their axes of rotation and axes of the mounting device. Since P6 will require centering of targets and retroreflectors on a tripod, an additional rotatable optical plummet (available from Wild) should be used. Otherwise, the optical plummet which is built into the Wild tribrachs should be carefully adjusted before each campaign and the centering of the target should be repeated between sets of angle measurements after rotating the tribrach on the tripod by 90^0 , each time.

Point c) above is extremely important in the case of steep lines of sight. For example, an error of 5" in levelling (which is only 1/4 of one division of the spirit level in T2000) in the direction of the trunnion

axis will cause an error of 1.8" in direction measurement if the line of sight is inclined 20°. The use of the compensator of the vertical circle may give the accuracy better than 1" in levelling the instrument. Here, a theodolite such as Kern E2 would be more convenient because it has a double compensator and provides automatic correction to the measured directions due to mislevelling of the instrument.

Regarding point d) above, these consultants would recommend using custom-made, special targets of a conical shape. They could certainly provide better pointing accuracy than the standard Wild targets which are not made for high precision engineering surveys. The custom-made targets would provide an additional advantage in that they would not require their rotation when sighting from different directions and hence decrease the required manpower. If the decision on the use of the Wild targets cannot be changed, the targets will have to be carefully checked and, the results of the first campaign, may indicate that the number of pointings will have to be increased.

The above specifications may prove to be either too rigorous or too lax. Only an a posteriori analysis of the results of the first campaign will show what changes in the field procedures will be needed in the subsequent campaigns. It depends on the experience and care of the survey crew as well as the actual physical conditions at the time of measurement.

The requirement of $\pm 5 \text{ mm} \pm 5 \text{ ppm}$ should be satisfied by the Wild DI4L instrument but only when the instrument is carefully calibrated prior to the first campaign and at least once in the middle and once after completing the project, for cyclic error, zero error and scale. Due to the comparatively short distances involved, the pointing of the instrument is

very critical because it may easily change the strength of the returning signal and introduce a bias into the phase measurements. It is recommended to take at least 15 readings of the EDM with separate electronic pointings to the reflector before each group of 5. Though the distances are short, use of good quality calibrated barometers and thermometers is recommended for meteorological corrections because some pocket barometers show errors as large as 20 mb which could introduce a significant change in scale of the measured distances and, consequently distort the deformation analysis. The scale calibration must be made on a calibrated baseline against measurements with more accurate instruments such as Kern Mekometer, Geomensor or, at least, Tellurometer MA100. Heights of the retroreflector on the tripod at P6 should always be measured to ± 0.001 m for the distance reductions.

Any calibration yields corrections to the instrument output that pertain to a specific EDM instrument and retroreflector combination. Ideally, the same combination should be used for each campaign, but if this is not possible, then calibration must be done for each combination before and after each campaign.

4.2 Design of Trigonometric Height Traversing

The vertical angle measurements, in order to achieve the 0.7" standard deviation must follow practically the same specifications as listed in 4.1 for horizontal directions. These would be easily met since the T2000 provides a simultaneous measurement of the horizontal and vertical circles. Shading of the instrument is extremely important.

Care must be taken that the heights of the theodolite and of the targets are the same in all campaigns or measurements of these heights must

be made with an accuracy better than 1 mm. This may be difficult to achieve on P6 where the target will be on a tripod. An auxiliary spirit level with a levelling staff could be used to measure the height of the target in each campaign.

As it was mentioned, the possible changes in the coefficient of refraction may cause major problems in achieving the required vertical accuracy. Reciprocal and simultaneous measurement of the vertical angles could decrease the refraction effect. However, this would significantly prolong the survey campaign and it would require additional instrumentation and its adaptation (Chrzanowski, 1985). Perhaps, as another possible remedy, these consultants recommend measuring gradients of temperature in the vicinity (say \sim 20 m in front of the instrument) near the instrument station along the lines of sight. The instrumentation for that purpose is available at UNB. From the changes of the gradients one could easily estimate the refraction error and even calculate approximate corrections (Chrzanowski, 1984).

5. CONCLUSIONS AND RECOMMENDATIONS

The main conclusion is that the required accuracy of 3 mm in detecting the dam movement can be met with the instruments available to the BSC group, namely the T2000 theodolite and DI4L EDM instrument. The use of the Wild targets may cause some problems. However, the analysis of the first campaign will provide sufficient evidence whether the desired accuracy can be met with these targets. If not, a redesign of the survey in the next campaign should not be difficult. UNB will gladly assist in the analysis of the survey.

It is estimated that the proposed survey scheme should allow completing one campaign in about 2 1/2 days by a survey crew of 3 if an electronic data collector would be available for the T2000. Practically, any microcomputer can easily be interfaced with the T2000. These consultants successfully used the TRS80 Model 100 and EPSON HX20 microcomputers. They are inexpensive ($\sim \$1000$ with printer and cassette recorder). They could provide a real-time check of the field data and even direct comparison of the measured angles and distances with previous campaigns. This would make the whole project run more smoothly and more economically. UNB could develop all the necessary software.

UNB has a Kern E2 theodolite with DM502 EDM instrument ($\pm 3 \text{ mm} \pm 2 \text{ ppm}$) interfaced with the TRS 80 Model 100 microcomputer. The use of the system could be made available to the project. Also one very experienced research assistant could participate in the field surveys. As mentioned before, UNB has instrumentation and expertise in the measurements of the gradients of temperature.

The UNB baseline (1.6 km long with 6 pillars and accuracy $\pm 1 \text{ mm}$) could be used for the calibration of the EDM equipment. All the software necessary for the processing of the calibration measurements (on any baseline) has been implemented at UNB.

The analysis of the deformation surveys could efficiently be made using the UNB Generalized Method. The Method would allow integrating the analysis of the geodetic surveys with the intended borehole measurements by inclinometers (Chrzanowski et al., 1985). There is no other method available which allows for such an integrated analysis. This would be very valuable for geotechnical engineers who will be in charge of the interpretation of the monitoring surveys.

6. REFERENCES

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BALL MOUNTAIN DAM, VERMONT 1.0; 0.005.5.0
THU, NOV. 28, 1985 15:47:54

OPTIONS IN EFFECT

PREANALYSIS OR ADJUSTMENT

PREANALYSIS

BLAHA STATIONS

WEIGHTED STATIONS

FIXED STATIONS

P1

CONVENTIONAL LINEAR UNIT

METRE

INITIAL APPROXIMATE COORDINATES

FREE STATIONS:

STATION	X (E)	Y (N)
P2	304.8000	21.3000
P3	474.0000	129.5000
P4	289.6000	390.1000
P5	128.0000	335.3000
P6	228.6000	115.8000
TOWER	77.7000	169.2000
A2	219.5000	192.0000
A5	280.4000	187.5000
A9	338.3000	181.4000
B2	242.3000	249.9000
B5	288.0000	240.8000
B9	338.3000	231.6000
C2	254.5000	300.2000
C5	295.7000	286.5000
C9	347.5000	272.8000

FIXED STATIONS:

STATION	X (E)	Y (N)
P1	97.5000	76.2000

SUMMARY OF INPUT OBSERVATIONS AND THEIR STANDARD DEVIATIONS:

	AT	FROM	TO	STD.DEV
DISTANCE	P4	P4	P3	0.005
DISTANCE	P4	P4	P2	0.005
DISTANCE	P4	P4	P6	0.005
DISTANCE	P4	P4	P1	0.005
DIRECTION 1	P1	P1	TOWER	1.00
DIRECTION 2	P1	P1	P5	1.00
DIRECTION 3	P1	P1	P4	1.00
DIRECTION 4	P1	P1	P6	1.00
DIRECTION 1	P2	P2	P6	1.00
DIRECTION 2	P2	P2	P5	1.00
DIRECTION 3	P2	P2	A2	1.00
DIRECTION 4	P2	P2	B2	1.00
DIRECTION 5	P2	P2	C2	1.00
DIRECTION 6	P2	P2	A5	1.00
DIRECTION 7	P2	P2	B5	1.00
DIRECTION 8	P2	P2	C5	1.00
DIRECTION 9	P2	P2	P4	1.00
DIRECTION 10	P2	P2	B9	1.00
DIRECTION 11	P2	P2	C9	1.00
DIRECTION 12	P2	P2	A9	1.00
DIRECTION 13	P2	P2	P3	1.00
DIRECTION 1	P3	P3	P2	1.00
DIRECTION 2	P3	P3	P6	1.00
DIRECTION 3	P3	P3	A5	1.00
DIRECTION 4	P3	P3	A9	1.00
DIRECTION 5	P3	P3	B5	1.00
DIRECTION 6	P3	P3	B9	1.00

DIRECTION	7	P3	P3	C5	1.00
DIRECTION	8	P3	P3	C9	1.00
DIRECTION	9	P3	P3	P4	1.00
DIRECTION	1	P4	P4	P3	1.00
DIRECTION	2	P4	P4	C9	1.00
DIRECTION	3	P4	P4	B9	1.00
DIRECTION	4	P4	P4	A9	1.00
DIRECTION	5	P4	P4	P2	1.00
DIRECTION	6	P4	P4	C5	1.00
DIRECTION	7	P4	P4	B5	1.00
DIRECTION	8	P4	P4	A5	1.00
DIRECTION	9	P4	P4	P6	1.00
DIRECTION	10	P4	P4	A2	1.00
DIRECTION	11	P4	P4	B2	1.00
DIRECTION	12	P4	P4	C2	1.00
DIRECTION	13	P4	P4	P1	1.00
DIRECTION	14	P4	P4	TOWER	1.00
DIRECTION	15	P4	P4	P5	1.00
DIRECTION	1	P5	P5	P4	1.00
DIRECTION	2	P5	P5	C2	1.00
DIRECTION	3	P5	P5	B2	1.00
DIRECTION	4	P5	P5	A2	1.00
DIRECTION	5	P5	P5	P2	1.00
DIRECTION	6	P5	P5	P6	1.00
DIRECTION	7	P5	P5	P1	1.00
DIRECTION	8	P5	P5	TOWER	1.00
AZIMUTH		P1	P1	P4	0.01

STATISTICS SUMMARY

	NUMBER OF OBSERVATIONS	NUMBER OF UNKNOWNS
DISTANCES	4	ZERO ERROR
DIRECTIONS	49	ORIENTATION
ANGLES	0	
AZIMUTHS	1	
COORDINATES	0	COORDINATES
TOTALS	54	35

THE NUMBER OF DEGREES OF FREEDOM IS 19

STATION 95.000 % CONFIDENCE ELLIPSES (METRES)

FACTOR USED FOR OBTAINING THESE ELLIPSES FROM STANDARD ELLIPSES: (VARIANCE FACTOR KNOWN) = 2.4484

STATION	SEMI-MAJOR AXIS	SEMI-MINOR AXIS	AZIMUTH OF SEMI-MAJOR AXIS	AREA OF ELLIPSE
P2	0.0054	0.0036	273 58 12	0.61235D-04
P3	0.0082	0.0039	71 2 29	0.99966D-04
P4	0.0075	0.0000	31 27 56	0.10258D-05
P5	0.0060	0.0022	14 42 51	0.42343D-04
P6	0.0042	0.0019	71 29 53	0.24896D-04
TOWER	0.0049	0.0014	352 1 17	0.20983D-04
A2	0.0051	0.0034	15 54 13	0.54215D-04
A5	0.0054	0.0033	42 35 18	0.55385D-04
A9	0.0060	0.0033	55 1 40	0.62581D-04
B2	0.0055	0.0023	32 59 5	0.40327D-04
B5	0.0062	0.0032	33 27 31	0.61388D-04
B9	0.0065	0.0039	42 32 42	0.79230D-04
C2	0.0062	0.0014	33 7 4	0.27874D-04
C5	0.0072	0.0033	24 59 47	0.74979D-04
C9	0.0071	0.0049	30 29 38	0.10897D-03

TOTAL AREA OF STATION ELLIPSES = 0.81640D-03

RELATIVE 95.000 % CONFIDENCE ELLIPSES (METRES)

FACTOR USED FOR OBTAINING THESE ELLIPSES FROM STANDARD ELLIPSES: (VARIANCE FACTOR KNOWN)							=	2.4484	
FROM	TO	SEMI-MAJOR	SEMI-MINOR	AZIMUTH	MAJOR	DISTANCE	PRECISION	STD.DEV.	STD.DEV.
								ADJ.DISTANCE	ADJ.AZIMUTH
P2	P3	0.0051	0.0029	51 34 36	200.8379	1:	39511	0.0021	1.24
P2	P4	0.0073	0.0035	356 4 49	369.1131	1:	50637	0.0030	0.80
P2	P5	0.0073	0.0045	326 25 10	360.3529	1:	49438	0.0030	1.05
P2	P6	0.0041	0.0020	312 43 50	121.3948	1:	29302	0.0017	1.42
P2	TOWER	0.0065	0.0054	340 11 6	271.0144	1:	41629	0.0025	1.82
P2	A2	0.0056	0.0030	336 53 54	190.8260	1:	34012	0.0023	1.34
P2	A5	0.0047	0.0027	347 24 2	167.9815	1:	35931	0.0019	1.34
P2	A9	0.0043	0.0027	5 5 47	163.5673	1:	36320	0.0017	1.40
P2	B2	0.0055	0.0032	344 54 34	236.9899	1:	43049	0.0024	1.14
P2	B5	0.0059	0.0030	352 27 34	220.1420	1:	37598	0.0024	1.16
P2	B9	0.0057	0.0032	355 37 26	212.9515	1:	37674	0.0023	1.33
P2	C2	0.0060	0.0034	350 17 12	283.3995	1:	47318	0.0024	1.00
P2	C5	0.0072	0.0032	354 38 57	265.3561	1:	36604	0.0030	1.01
P2	C9	0.0070	0.0037	349 17 1	265.0991	1:	36405	0.0027	1.40
P2	P4	0.0065	0.0038	328 19 12	319.2424	1:	49273	0.0026	1.02
P3	P5	0.0081	0.0053	293 38 56	402.5787	1:	49594	0.0033	1.12
P3	P6	0.0058	0.0038	82 33 45	245.7821	1:	42557	0.0024	1.29
P3	TOWER	0.0083	0.0068	74 23 19	398.2835	1:	47934	0.0033	1.49
P3	A2	0.0060	0.0054	311 43 30	262.0620	1:	43517	0.0024	1.79
P3	A5	0.0049	0.0037	290 49 25	202.1014	1:	41542	0.0020	1.56
P3	A9	0.0039	0.0027	290 25 20	145.2863	1:	36985	0.0016	1.56
P3	B2	0.0057	0.0048	308 45 47	261.1150	1:	45822	0.0023	1.56
P3	B5	0.0055	0.0038	319 4 20	216.7572	1:	39548	0.0022	1.57
P3	B9	0.0050	0.0030	316 40 51	169.8202	1:	33722	0.0024	1.53
P3	C2	0.0058	0.0045	315 48 56	278.0625	1:	47703	0.0024	1.38
P3	C5	0.0067	0.0039	334 7 57	237.5708	1:	35455	0.0026	1.56
P3	C9	0.0064	0.0032	326 6 23	191.1469	1:	29679	0.0026	1.44
P4	P5	0.0044	0.0018	63 34 43	170.6388	1:	39116	0.0018	0.91
P4	P6	0.0056	0.0026	12 0 56	281.0009	1:	50535	0.0023	0.78
P4	TOWER	0.0073	0.0033	28 28 27	306.1020	1:	41989	0.0029	1.02
P4	A2	0.0055	0.0027	2 43 0	210.1371	1:	38083	0.0022	1.22
P4	A5	0.0050	0.0023	357 17 21	202.8088	1:	40818	0.0020	0.97
P4	A9	0.0050	0.0024	346 40 2	214.3067	1:	43228	0.0020	0.92
P4	B2	0.0039	0.0020	9 43 59	147.9639	1:	37629	0.0022	1.17
P4	B5	0.0047	0.0019	355 37 38	149.3086	1:	31491	0.0019	1.09
P4	B9	0.0050	0.0020	342 18 21	165.8130	1:	32991	0.0021	1.02
P4	C2	0.0029	0.0014	20 19 19	96.5092	1:	33215	0.0012	1.18
P4	C5	0.0053	0.0014	354 13 55	103.7794	1:	19553	0.0022	1.16
P4	C9	0.0058	0.0017	336 44 56	130.8117	1:	22633	0.0024	1.11
P4	P6	0.0053	0.0023	308 42 44	142.6802	1:	45913	0.0016	1.18
P5	B2	0.0060	0.0024	13 40 4	173.6491	1:	37497	0.0019	2.02
P5	B5	0.0050	0.0017	329 46 0	170.0210	1:	41398	0.0023	1.64
P5	B9	0.0057	0.0044	315 0 53	234.4777	1:	37450	0.0014	1.37
P5	A2	0.0052	0.0020	270 1 7	131.2793	1:	31216	0.0018	2.62
P5	C2	0.0035	0.0042	308 21 30	260.6560	1:	35945	0.0024	1.97
P5	C5	0.0056	0.0042	364 23 46	174.6560	1:	228.2247	0.0017	2.77
P5	C9	0.0063	0.0047	322 51 5	160.0699	1:	30269	0.0017	2.55
P6	TOWER	0.0053	0.0042	9 15 50	167.7414	1:	16241	0.0019	
P6	A2	0.0047	0.0022	341 5 24					

3.15	0.0013	88	4541	1:
P6	A5	127.	.8180	1:
P6	A9	134.	.7980	1:
P6	B2	138.	.3957	1:
P6	B5	159.	.5109	1:
P6	B9	186.	.2100	1:
P6	C2	183.	.4146	1:
P6	C5	196.	.9421	1:
P6	C9	143.	.6213	1:
P6	TOWER	203.	.5244	1:
TOWER	A5	260.	.8854	1:
TOWER	A9	260.	.8854	1:
TOWER	B2	260.	.8854	1:
TOWER	B5	267.	.9665	1:
TOWER	B9	270.	.0437	1:
TOWER	C2	270.	.6227	1:
TOWER	C5	270.	.2274	1:
TOWER	C9	270.	.1052	1:
TOWER	TOWFR	270.	.2262	1:
A2	A5	347.	6.10	1:
A2	A9	347.	3.7	1:
A2	B2	343.	4.8	1:
A2	B5	352.	1.9	3
A2	B9	347.	3.2	0
A2	C2	352.	2.2	30
A2	C5	355.	0	53
A2	C9	344.	32	39
A2	A9	339.	28	0
A2	B9	350.	4.5	2
A2	C5	349.	27	59
A2	C9	342.	5.9	47
A2	A9	354.	2.5	48
A2	B5	352.	5.9	46
A2	B9	340.	28	41
A2	C5	345.	39	18
A2	C9	343.	1	27
A2	A9	337.	0	54
A2	B5	346.	4	50
A2	B9	348.	6	35
A2	C5	336.	54	26
A2	C9	354.	4	52
A2	A9	346.	6	23
A2	B5	357.	5	26
A2	B9	356.	11	39
A2	C5	341.	42	31
A2	C9	341.	4	4
A2	A9	356.	3	3
A2	B5	351.	41	21
A2	B9	351.	4	19
A2	C5	338.	49	12
A2	C9	344.	51	46
A2	A9	345.	36	27
A2	B5	345.	0	20
A2	B9	356.	0	19
A2	C5	351.	0	18
A2	C9	356.	4	6
A2	A9	339.	32	52
A2	B5	344.	0	26
A2	B9	351.	0	22
A2	C5	344.	0	17
A2	C9	353.	25	12

2

* BALL MOUNTAIN DAM, VERMONT 0.5; 0.005.5.0
* *****
* THU, NOV. 28, 1985 17:32:08

OPTIONS IN EFFECT

PREANALYSIS OR ADJUSTMENT PREANALYSIS

WEIGHTED STATIONS

BLAHA STATIONS

FIXED STATIONS

P1

CONVENTIONAL LINEAR UNIT METRE

INITIAL APPROXIMATE COORDINATES

FREE STATIONS:

STATION	X (E)	Y (N)
P2	304.8000	21.3000
P3	474.0000	129.5000
P4	289.6000	390.1000
P5	128.0000	335.3000
P6	228.6000	115.8000
TOWER	77.7000	169.2000
A2	219.5000	192.0000
A5	280.4000	187.5000
A9	338.3000	181.4000
B2	242.3000	249.9000
B5	288.0000	240.8000
B9	338.3000	231.6000
C2	264.5000	300.2000
C5	295.7000	286.5000
C9	347.6000	272.8000

FIXED STATIONS:

STATION	X (E)	Y (N)
P1	97.5000	76.2000

SUMMARY OF INPUT OBSERVATIONS AND THEIR STANDARD DEVIATIONS:

	AT	FROM	TO	STD.DEV
DISTANCE	P4	P4	P3	0.005
DISTANCE	P4	P4	P2	0.005
DISTANCE	P4	P4	P6	0.005
DISTANCE	P4	P4	P1	0.005
DIRECTION 1	P1	P1	TOWER	0.50
DIRECTION 2	P1	P1	P5	0.50
DIRECTION 3	P1	P1	P4	0.50
DIRECTION 4	P1	P1	P6	0.50
DIRECTION 1	P2	P2	P6	0.50
DIRECTION 2	P2	P2	P5	0.50
DIRECTION 3	P2	P2	A2	0.50
DIRECTION 4	P2	P2	B2	0.50
DIRECTION 5	P2	P2	C2	0.50
DIRECTION 6	P2	P2	A5	0.50
DIRECTION 7	P2	P2	B5	0.50
DIRECTION 8	P2	P2	C5	0.50
DIRECTION 9	P2	P2	P4	0.50
DIRECTION 10	P2	P2	B9	0.50
DIRECTION 11	P2	P2	C9	0.50
DIRECTION 12	P2	P2	A9	0.50
DIRECTION 13	P2	P2	P3	0.50
DIRECTION 1	P3	P3	P2	0.50
DIRECTION 2	P3	P3	P6	0.50
DIRECTION 3	P3	P3	A5	0.50
DIRECTION 4	P3	P3	A9	0.50
DIRECTION 5	P3	P3	B5	0.50
DIRECTION 6	P3	P3	B9	0.50

DIRECTION	7	P3	P3	C5	0.50
DIRECTION	8	P3	P3	C9	0.50
DIRECTION	9	P3	P3	P4	0.50
DIRECTION	1	P4	P4	P3	0.50
DIRECTION	2	P4	P4	C9	0.50
DIRECTION	3	P4	P4	B9	0.50
DIRECTION	4	P4	P4	A9	0.50
DIRECTION	5	P4	P4	P2	0.50
DIRECTION	6	P4	P4	C5	0.50
DIRECTION	7	P4	P4	B5	0.50
DIRECTION	8	P4	P4	A5	0.50
DIRECTION	9	P4	P4	P6	0.50
DIRECTION	10	P4	P4	A2	0.50
DIRECTION	11	P4	P4	B2	0.50
DIRECTION	12	P4	P4	C2	0.50
DIRECTION	13	P4	P4	P1	0.50
DIRECTION	14	P4	P4	TOWER	0.50
DIRECTION	15	P4	P4	P5	0.50
DIRECTION	1	P5	P5	P4	0.50
DIRECTION	2	P5	P5	C2	0.50
DIRECTION	3	P5	P5	B2	0.50
DIRECTION	4	P5	P5	A2	0.50
DIRECTION	5	P5	P5	P2	0.50
DIRECTION	6	P5	P5	P6	0.50
DIRECTION	7	P5	P5	P1	0.50
DIRECTION	8	P5	P5	TOWER	0.50
AZIMUTH		P1	P1	P4	0.01

STATISTICS SUMMARY

	NUMBER OF OBSERVATIONS	NUMBER OF UNKNOWNS
DISTANCES	4	ZERO ERROR
DIRECTIONS	49	ORIENTATION
ANGLES	0	
AZIMUTHS	1	
COORDINATES	0	COORDINATES
TOTALS	54	36

THE NUMBER OF DEGREES OF FREEDOM IS 19

STATION 95.000 % CONFIDENCE ELLIPSES (METRES)

FACTOR USED FOR OBTAINING THESE ELLIPSES FROM STANDARD ELLIPSES: (VARIANCE FACTOR KNOWN) = 2.4484

STATION	SEMI-MAJOR AXIS	SEMI-MINOR AXIS	AZIMUTH OF SEMI-MAJOR AXIS	AREA OF ELLIPSE
P2	0.0045	0.0019	282	9 56 0.26163D-04
P3	0.0075	0.0021	79	12 28 0.48705D-04
P4	0.0072	0.0000	31	27 56 0.98615D-06
P5	0.0053	0.0012	9	5 21 0.19342D-04
P6	0.0031	0.0009	72	22 28 0.92318D-05
TOWER	0.0029	0.0007	350	47 2 0.62882D-05
A2	0.0037	0.0019	37	35 3 0.21945D-04
A5	0.0044	0.0017	54	23 36 0.24096D-04
A9	0.0053	0.0017	63	29 9 0.28765D-04
B2	0.0047	0.0012	37	44 59 0.17546D-04
B5	0.0052	0.0017	44	42 59 0.27653D-04
B9	0.0057	0.0020	53	49 54 0.36817D-04
C2	0.0055	0.0007	34	26 18 0.12516D-04
C5	0.0059	0.0019	37	50 38 0.34857D-04
C9	0.0063	0.0026	47	49 30 0.51442D-04

TOTAL AREA OF STATION ELLIPSES = 0.36635D-03

RELATIVE 95.000 % CONFIDENCE ELLIPSES (METRES)

FACTOR USED FOR OBTAINING THESE ELLIPSES FROM STANDARD ELLIPSES: (VARIANCE FACTOR KNOWN) = 2.4484									
FROM	TO	SEMI-MAJOR	SEMI-MINOR	AZIMUTH	MAJOR	DISTANCE	PRECISION	STD.DEV.	STD.DEV.
							ADJ.DISTANCE	ADJ.	AZIMUTH
P2	P3	0.0042	0.0015	55 45 33	200.8379	1:	478.31	0.0017	0.62
P2	P4	0.0072	0.0018	357 18 5	369.1131	1:	516.23	0.0029	0.40
P2	P5	0.0070	0.0022	329 50 20	360.3529	1:	513.16	0.0029	0.52
P2	P6	0.0029	0.0010	317 28 20	121.3948	1:	418.71	0.0012	0.71
P2	TOWER	0.0055	0.0029	307 19 9	271.0144	1:	495.23	0.0022	0.92
P2	A2	0.0042	0.0015	334 41 17	190.8260	1:	449.93	0.0017	0.67
P2	A5	0.0036	0.0013	350 16 48	167.9815	1:	460.73	0.0015	0.67
P2	A9	0.0035	0.0014	10 0 6	163.5673	1:	472.94	0.0014	0.70
P2	B2	0.0048	0.0016	344 45 30	236.9899	1:	492.10	0.0020	0.57
P2	B5	0.0047	0.0015	354 36 29	220.1420	1:	469.06	0.0019	0.58
P2	B9	0.0045	0.0017	5 2 18	212.9515	1:	471.73	0.0018	0.67
P2	C2	0.0056	0.0017	349 52 62	283.3995	1:	506.67	0.0023	0.50
P2	C5	0.0057	0.0016	366 49 66	265.3561	1:	464.12	0.0023	0.51
P2	C9	0.0054	0.0020	3 4 40	255.0991	1:	468.78	0.0022	0.70
P2	P4	0.0062	0.0019	325 25 53	319.2424	1:	512.46	0.0025	0.51
P3	P5	0.0078	0.0027	299 32 17	402.5787	1:	513.92	0.0032	0.56
P3	P6	0.0050	0.0019	85 56 47	245.7821	1:	490.48	0.0020	0.65
P3	P3	0.0078	0.0035	273 27 51	398.2835	1:	511.45	0.0032	0.75
P3	A2	0.0053	0.0028	285 51 54	262.0620	1:	497.04	0.0022	0.90
P3	A5	0.0042	0.0019	287 26 9	202.1014	1:	486.55	0.0017	0.78
P3	A9	0.0031	0.0013	290 49 44	145.2863	1:	465.98	0.0013	0.78
P3	B2	0.0052	0.0024	298 44 17	261.1150	1:	502.60	0.0021	0.78
P3	B5	0.0045	0.0020	304 56 9	216.7572	1:	481.30	0.0018	0.79
P3	B9	0.0038	0.0015	310 15 25	169.8202	1:	449.40	0.0015	0.77
P3	C2	0.0055	0.0023	308 59 1	278.0625	1:	508.22	0.0022	0.69
P3	C5	0.0051	0.0021	318 35 20	237.5708	1:	464.56	0.0021	0.78
P3	C9	0.0045	0.0016	321 52 43	191.1469	1:	422.65	0.0018	0.72
P3	P5	0.0036	0.0009	68 44 18	170.6388	1:	477.01	0.0015	0.45
P4	P6	0.0054	0.0013	12 24 54	281.0099	1:	515.98	0.0022	0.39
P4	TOWER	0.0062	0.0018	39 25 47	306.1020	1:	491.23	0.0025	0.51
P4	A2	0.0044	0.0015	14 11 4	210.1371	1:	475.38	0.0018	0.61
P4	A5	0.0042	0.0012	1 0 58	202.8088	1:	483.89	0.0017	0.49
P4	A9	0.0043	0.0012	346 48 13	214.3067	1:	492.85	0.0018	0.46
P4	B2	0.0031	0.0010	12 47 27	147.9639	1:	470.31	0.0013	0.59
P4	B5	0.0034	0.0010	358 27 20	149.3086	1:	434.84	0.0014	0.66
P4	B9	0.0037	0.0010	342 39 39	165.8130	1:	443.88	0.0015	0.61
P4	C2	0.0022	0.0007	20 56 9	96.5092	1:	445.31	0.0009	0.59
P4	C5	0.0032	0.0007	354 59 11	103.7794	1:	327.68	0.0013	0.58
P4	C9	0.0036	0.0009	334 57 59	130.8117	1:	361.38	0.0015	0.56
P4	P6	0.0048	0.0017	336 2 17	241.4552	1:	502.28	0.0020	0.59
P5	TOWER	0.0042	0.0012	15 22 58	173.5491	1:	417.75	0.0017	0.59
P5	A2	0.0038	0.0014	328 18 10	170.0210	1:	443.96	0.0016	0.68
P5	A5	0.0044	0.0020	316 33 6	212.2984	1:	486.78	0.0018	0.79
P5	A9	0.0052	0.0021	306 33 12	260.5980	1:	502.19	0.0021	0.68
P5	B2	0.0031	0.0012	305 34 16	142.6802	1:	466.93	0.0012	0.69
P5	B5	0.0039	0.0022	305 37 19	185.8232	1:	477.84	0.0016	1.01
P5	B9	0.0048	0.0023	299 18 51	234.4777	1:	488.78	0.0020	0.82
P5	C2	0.0028	0.0010	280 51 57	131.2793	1:	471.44	0.0011	0.68
P5	C5	0.0037	0.0027	296 40 34	174.6560	1:	473.12	0.0015	1.31
P5	C9	0.0048	0.0026	293 50 30	228.2247	1:	474.18	0.0020	0.98
P5	TOWER	0.0034	0.0026	294 55 4	160.0699	1:	470.50	0.0014	1.39
P6	A2	0.0027	0.0011	344 16 39	286.4714	1:	344.77	0.0011	1.28

3

*** BALL MOUNTAIN DAM, VERMONT 0.5; 0.003,2.0

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OPTIONS IN EFFECT

PREANALYSIS OR ADJUSTMENT PREANALYSIS

FIXED STATIONS
P1

WEIGHTED STATIONS

CONVENTIONAL LINEAR UNIT METRE

INITIAL APPROXIMATE COORDINATES

FREE STATIONS:

STATION	X (E)	Y (N)
P2	304.8000	21.3000
P3	474.0000	129.5000
P4	289.6000	390.1000
P5	128.0000	335.3000
P6	228.6000	115.8000
TOWER	77.7000	169.2000
A2	219.5000	192.0000
A5	280.4000	187.5000
A9	338.3000	181.4000
B2	242.3000	249.9000
B5	268.0000	240.8000
B9	338.3000	231.6000
C2	254.5000	300.2000
C5	295.7000	286.5000
C9	347.5000	272.8000

FIXED STATIONS:

STATION	X (E)	Y (N)
P1	97.5000	76.2000

SUMMARY OF INPUT OBSERVATIONS AND THEIR STANDARD DEVIATIONS:

	AT	FROM	TO	STD. DEV.
DISTANCE	P4	P4	P3	0.003
DISTANCE	P4	P4	P2	0.003
DISTANCE	P4	P4	P6	0.003
DISTANCE	P4	P4	P1	0.003
DIRECTION	1	P1	P1	TOWER
DIRECTION	2	P1	P1	P5
DIRECTION	3	P1	P1	P4
DIRECTION	4	P1	P1	P6
DIRECTION	1	P2	P2	P6
DIRECTION	2	P2	P2	P5
DIRECTION	3	P2	P2	A2
DIRECTION	4	P2	P2	B2
DIRECTION	5	P2	P2	C2
DIRECTION	6	P2	P2	A5
DIRECTION	7	P2	P2	B5
DIRECTION	8	P2	P2	C5
DIRECTION	9	P2	P2	P4
DIRECTION	10	P2	P2	B9
DIRECTION	11	P2	P2	C9
DIRECTION	12	P2	P2	A9
DIRECTION	13	P2	P2	P3
DIRECTION	1	P3	P3	P2
DIRECTION	2	P3	P3	P6
DIRECTION	3	P3	P3	A5
DIRECTION	4	P3	P3	A9
DIRECTION	5	P3	P3	B5
DIRECTION	6	P3	P3	B9

DIRECTION	7	P3	P3	C5	0.50
DIRECTION	8	P3	P3	C9	0.50
DIRECTION	9	P3	P3	P4	0.50
DIRECTION	1	P4	P4	P3	0.50
DIRECTION	2	P4	P4	C9	0.50
DIRECTION	3	P4	P4	B9	0.50
DIRECTION	4	P4	P4	A9	0.50
DIRECTION	5	P4	P4	P2	0.50
DIRECTION	6	P4	P4	C5	0.50
DIRECTION	7	P4	P4	B5	0.50
DIRECTION	8	P4	P4	A5	0.50
DIRECTION	9	P4	P4	P6	0.50
DIRECTION	10	P4	P4	A2	0.50
DIRECTION	11	P4	P4	B2	0.50
DIRECTION	12	P4	P4	C2	0.50
DIRECTION	13	P4	P4	P1	0.50
DIRECTION	14	P4	P4	TOWER	0.50
DIRECTION	15	P4	P4	P5	0.50
DIRECTION	1	P5	P5	P4	0.50
DIRECTION	2	P5	P5	C2	0.50
DIRECTION	3	P5	P5	B2	0.50
DIRECTION	4	P5	P5	A2	0.50
DIRECTION	5	P5	P5	P2	0.50
DIRECTION	6	P5	P5	P6	0.50
DIRECTION	7	P5	P5	P1	0.50
DIRECTION	8	P5	P5	TOWER	0.50
AZIMUTH		P1	P1	P4	0.01

STATISTICS SUMMARY

NUMBER OF OBSERVATIONS	NUMBER OF UNKNOWNS
DISTANCES	4
DIRECTIONS	49
ANGLES	0
AZIMUTHS	1
COORDINATES	0
TOTALS	64
	35

THE NUMBER OF DEGREES OF FREEDOM IS 19

STATION 95.000 % CONFIDENCE ELLIPSES (METRES)

FACTOR USED FOR OBTAINING THESE ELLIPSES FROM STANDARD ELLIPSES: (VARIANCE FACTOR KNOWN) = 2.4484

STATION	SEMI-MAJOR AXIS	SEMI-MINOR AXIS	AZIMUTH OF SEMI-MAJOR AXIS	AREA OF ELLIPSE
P2	0.00030	0.0018	276 47 40	0.16984D-04
P3	0.00046	0.0020	73 50 45	0.28852D-04
P4	0.00043	0.0000	31 27 56	0.58939D-06
P5	0.00034	0.0011	12 58 25	0.11970D-04
P6	0.00023	0.0009	71 40 27	0.66630D-05
TOWER	0.00025	0.0007	351 49 20	0.53810D-05
A2	0.00027	0.0018	21 48 0	0.14811D-04
A5	0.00029	0.0017	46 24 57	0.15430D-04
A9	0.00034	0.0017	57 53 30	0.17723D-04
B2	0.00030	0.0012	34 26 39	0.11236D-04
B5	0.00034	0.0016	36 57 27	0.17277D-04
B9	0.00036	0.0020	46 37 38	0.22512D-04
C2	0.00035	0.0007	33 31 7	0.78418D-05
C5	0.00039	0.0017	28 47 27	0.21308D-04
C9	0.00040	0.0025	37 20 21	0.31119D-04

TOTAL AREA OF STATION ELLIPSES = 0.22970D-03

RELATIVE 95.000 % CONFIDENCE ELLIPSES (METRES)

FACTOR USED FOR OBTAINING THESE ELLIPSES FROM STANDARD ELLIPSES: (VARIANCE FACTOR KNOWN) = 2.4484

FROM	TO	SEMI-MAJOR	SEMI-MINOR	AZIMUTH	MAJOR	DISTANCE	PRECISION	STD.DEV.	ADJ.DISTANCE	STD.DEV.	ADJ.AZIMUTH
P2	P3	0.0028	0.0015	52 56	6	200.8379	1:	72013	0.0011	0.62	
P2	P4	0.0042	0.0018	356 33	23	369.1131	1:	87551	0.0017	0.40	
P2	P5	0.0042	0.0022	327 51	59	360.3529	1:	86029	0.0017	0.52	
P2	P6	0.0022	0.0010	313 52	37	121.3948	1:	55487	0.0009	0.71	
P2	TOWER	0.0035	0.0028	324 58	34	271.0144	1:	76730	0.0014	0.91	
P2	A2	0.0030	0.0015	336 18	21	190.8260	1:	63353	0.0012	0.67	
P2	A5	0.0025	0.0013	348 15	10	167.9815	1:	66447	0.0010	0.67	
P2	A9	0.0023	0.0014	34 6	31	163.5673	1:	70209	0.0009	0.70	
P2	B2	0.0031	0.0016	344 51	58	236.9899	1:	77157	0.0013	0.57	
P2	B5	0.0032	0.0015	353 5	57	220.1420	1:	69043	0.0013	0.58	
P2	B9	0.0031	0.0016	358 28	22	212.9515	1:	69390	0.0012	0.67	
P2	C2	0.0034	0.0017	350 8	10	283.3995	1:	83141	0.0014	0.50	
P2	C5	0.0039	0.0016	355 15	8	265.3561	1:	67491	0.0016	0.51	
P2	C9	0.0038	0.0019	353 5	18	255.0991	1:	67679	0.0015	0.70	
P2	P4	0.0037	0.0019	327 9	35	319.2424	1:	85754	0.0015	0.51	
P2	P5	0.0047	0.0027	296 14	50	402.5787	1:	86299	0.0019	0.56	
P2	P6	0.0032	0.0019	83 53	55	245.7821	1:	76486	0.0013	0.65	
P2	TOWER	0.0047	0.0035	84 40	31	398.2835	1:	84698	0.0019	0.75	
P3	A2	0.0033	0.0028	295 47	19	262.0620	1:	78617	0.0014	0.90	
P3	A5	0.0027	0.0019	289 24	2	202.1014	1:	75003	0.0011	0.78	
P3	A9	0.0021	0.0013	290 35	41	145.2863	1:	68078	0.0009	0.78	
P3	B2	0.0032	0.0024	303 21	8	261.1150	1:	81239	0.0013	0.78	
P3	B5	0.0030	0.0020	313 59	34	216.7572	1:	72422	0.0012	0.78	
P3	B9	0.0027	0.0015	314 53	49	169.8202	1:	62971	0.0011	0.77	
P3	C2	0.0033	0.0023	312 28	47	278.0625	1:	83737	0.0014	0.69	
P3	C5	0.0036	0.0020	329 52	43	237.5708	1:	66210	0.0014	0.78	
P3	C9	0.0034	0.0016	325 8	6	191.1469	1:	56213	0.0014	0.78	
P4	P5	0.0024	0.0009	65 3	48	170.6388	1:	71461	0.0010	0.45	
P4	P6	0.0032	0.0013	12 9	54	281.0009	1:	87412	0.0013	0.39	
P4	TOWER	0.0040	0.0017	31 52	0	306.1020	1:	76013	0.0016	0.51	
P4	A2	0.0030	0.0014	5 59	25	210.1371	1:	70174	0.0012	0.61	
P4	A5	0.0027	0.0012	358 26	47	202.8088	1:	73960	0.0011	0.49	
P4	A9	0.0028	0.0012	346 42	49	214.3067	1:	77422	0.0011	0.46	
P4	B2	0.0021	0.0010	11 30	21	147.9639	1:	69198	0.0009	0.59	
P4	B5	0.0025	0.0010	356 17	50	149.3086	1:	59252	0.0010	0.55	
P4	B9	0.0027	0.0010	342 23	35	165.8130	1:	61696	0.0011	0.51	
P4	C2	0.0016	0.0007	28 55	57	170.0210	1:	62074	0.0006	0.59	
P4	C5	0.0027	0.0007	354 21	26	103.7794	1:	38158	0.0011	0.58	
P4	C9	0.0030	0.0009	335 36	27	130.8117	1:	43809	0.0012	0.56	
P4	P6	0.0030	0.0017	337 40	38	241.4552	1:	81222	0.0012	0.59	
P5	TOWER	0.0031	0.0012	14 3	51	173.5491	1:	55279	0.0013	0.61	
P5	A2	0.0028	0.0014	329 22	57	170.0210	1:	61701	0.0011	0.68	
P5	A5	0.0028	0.0020	322 58	46	212.2984	1:	74763	0.0012	0.79	
P5	A9	0.0032	0.0021	307 33	59	260.5980	1:	81165	0.0013	0.68	
P5	B2	0.0021	0.0012	303 36	41	142.6802	1:	68343	0.0009	0.69	
P5	B5	0.0026	0.0021	324 26	2	185.8232	1:	70279	0.0010	1.01	
P5	B9	0.0031	0.0022	308 14	50	234.4777	1:	75252	0.0013	0.82	
P5	C2	0.0019	0.0010	273 15	25	131.2793	1:	69122	0.0008	0.68	
P5	C5	0.0028	0.0023	346 59	5	174.6556	1:	61708	0.0010	1.31	
P5	C9	0.0034	0.0024	313 59	19	228.2247	1:	67885	0.0013	0.98	
P5	TOWER	0.0027	0.0023	5 5	51	160.0699	1:	60317	0.0009	1.38	
P6	A2	0.0024	0.0011	341 34	18	76.7414	1:	31940	0.0010	1.28	

P6	P6	A5	A9	0.0019	88.4541	1:	1.58
P6	P6	B2	B2	0.0022	127.8180	1:	1.15
P6	P6	B5	B5	0.0024	134.7980	1:	0.78
P6	P6	B9	B9	0.0024	138.3957	1:	0.0009
P6	P6	C2	C2	0.0025	159.5109	1:	1.09
P6	P6	C5	C5	0.0031	186.2100	1:	0.55
P6	P6	C9	C9	0.0031	183.4146	1:	0.76
P6	P6	TOWER	TOWER	0.0012	196.9421	1:	1.09
P6	P6	A5	A5	0.0014	143.6213	1:	1.74
P6	P6	B9	B9	0.0018	203.5244	1:	1.25
P6	P6	C2	C2	0.0012	260.8854	1:	1.00
P6	P6	TOWER	TOWER	0.0014	183.3184	1:	1.10
P6	P6	B2	B2	0.0019	26.4137	1:	0.06
P6	P6	B5	B5	0.0030	25.816	1:	1.15
P6	P6	B9	B9	0.0035	35.3348	1:	0.0009
P6	P6	C2	C2	0.0026	35.355	1:	0.0014
P6	P6	TOWER	TOWER	0.0025	23.73	1:	0.011
P6	P6	A9	A9	0.0018	31.219	1:	0.013
P6	P6	C5	C5	0.0029	48.139	1:	0.0013
P6	P6	TOWER	TOWER	0.0012	20.4530	1:	1.08
P6	P6	B2	B2	0.0014	247.5546	1:	1.06
P6	P6	B5	B5	0.0019	26.4137	1:	1.10
P6	P6	B9	B9	0.0019	183.4146	1:	1.09
P6	P6	C9	C9	0.0031	196.9421	1:	1.74
A2	A2	A5	A5	0.0021	143.6213	1:	1.25
A2	A2	A9	A9	0.0021	203.5244	1:	1.00
A2	A2	B2	B2	0.0017	220.0437	1:	0.78
A2	A2	B5	B5	0.0014	247.5546	1:	1.08
A2	A2	B9	B9	0.0014	260.8854	1:	1.06
A2	A2	C2	C2	0.0024	26.4137	1:	1.10
A2	A2	C5	C5	0.0024	25.816	1:	1.15
A2	A2	C9	C9	0.0035	35.3348	1:	0.0009
A2	A2	A9	A9	0.0017	35.355	1:	0.0008
A2	A2	B9	B9	0.0030	23.510	1:	0.0007
A2	A2	C2	C2	0.0023	34.6438	1:	3.51
A2	A2	C5	C5	0.0026	34.6438	1:	1.80
A2	A2	C9	C9	0.0027	34.33243	1:	1.03
A2	A2	A9	A9	0.0017	34.44846	1:	2.10
A2	A2	B2	B2	0.0011	62.2274	1:	2.62
A2	A2	B5	B5	0.0014	84.1052	1:	2.00
A2	A2	B9	B9	0.0014	125.2262	1:	1.05
A2	A2	C2	C2	0.0018	248.669	1:	1.05
A2	A2	C5	C5	0.0018	248.669	1:	1.05
A2	A2	C9	C9	0.0032	248.669	1:	1.05
A2	A2	A9	A9	0.0012	113.7200	1:	1.75
A2	A2	B9	B9	0.0012	113.7200	1:	1.75
A2	A2	C2	C2	0.0012	113.7200	1:	1.75
A2	A2	C5	C5	0.0012	113.7200	1:	1.75
A2	A2	C9	C9	0.0012	113.7200	1:	1.75
A2	A2	A9	A9	0.0014	113.7200	1:	1.75
A2	A2	B9	B9	0.0014	113.7200	1:	1.75
A2	A2	C2	C2	0.0014	113.7200	1:	1.75
A2	A2	C5	C5	0.0014	113.7200	1:	1.75
A2	A2	C9	C9	0.0014	113.7200	1:	1.75
A2	A2	A9	A9	0.0017	113.7200	1:	1.75
A2	A2	B9	B9	0.0017	113.7200	1:	1.75
A2	A2	C2	C2	0.0017	113.7200	1:	1.75
A2	A2	C5	C5	0.0017	113.7200	1:	1.75
A2	A2	C9	C9	0.0017	113.7200	1:	1.75
A5	A5	A5	A5	0.0023	34.650	1:	3.51
A5	A5	B5	B5	0.0023	35.52759	1:	1.80
A5	A5	C5	C5	0.0034	35.52759	1:	1.80
A5	A5	A9	A9	0.0023	35.52759	1:	1.80
A5	A5	B9	B9	0.0023	35.52759	1:	1.80
A5	A5	C9	C9	0.0035	35.52759	1:	1.80
A5	A5	A9	A9	0.0019	34.55613	1:	1.89
A5	A5	B9	B9	0.0019	34.55613	1:	1.89
A5	A5	C2	C2	0.0019	34.55613	1:	1.89
A5	A5	C5	C5	0.0019	34.55613	1:	1.89
A5	A5	C9	C9	0.0019	34.55613	1:	1.89
A5	A5	A9	A9	0.0012	153.310	1:	2.34
A5	A5	B9	B9	0.0012	153.310	1:	2.34
A5	A5	C2	C2	0.0012	153.310	1:	2.34
A5	A5	C5	C5	0.0012	153.310	1:	2.34
A5	A5	C9	C9	0.0012	153.310	1:	2.34
A5	A5	A9	A9	0.0015	34.5568	1:	1.90
A5	A5	B9	B9	0.0015	34.5568	1:	1.90
A5	A5	C2	C2	0.0015	34.5568	1:	1.90
A5	A5	C5	C5	0.0015	34.5568	1:	1.90
A5	A5	C9	C9	0.0015	34.5568	1:	1.90
A5	A5	A9	A9	0.0023	34.5568	1:	1.90
A5	A5	B9	B9	0.0023	34.5568	1:	1.90
A5	A5	C2	C2	0.0023	34.5568	1:	1.90
A5	A5	C5	C5	0.0023	34.5568	1:	1.90
A5	A5	C9	C9	0.0023	34.5568	1:	1.90
A5	A5	A9	A9	0.0021	34.54914	1:	2.34
A5	A5	B9	B9	0.0021	34.54914	1:	2.34
A5	A5	C2	C2	0.0021	34.54914	1:	2.34
A5	A5	C5	C5	0.0021	34.54914	1:	2.34
A5	A5	C9	C9	0.0021	34.54914	1:	2.34
A5	A5	A9	A9	0.0019	34.54914	1:	2.34
A5	A5	B9	B9	0.0019	34.54914	1:	2.34
A5	A5	C2	C2	0.0019	34.54914	1:	2.34
A5	A5	C5	C5	0.0019	34.54914	1:	2.34
A5	A5	C9	C9	0.0019	34.54914	1:	2.34
A5	A5	A9	A9	0.0014	34.54914	1:	2.34
A5	A5	B9	B9	0.0014	34.54914	1:	2.34
A5	A5	C2	C2	0.0014	34.54914	1:	2.34
A5	A5	C5	C5	0.0014	34.54914	1:	2.34
A5	A5	C9	C9	0.0014	34.54914	1:	2.34
B2	B2	B2	B2	0.0027	34.5568	1:	3.39
B2	B2	B5	B5	0.0024	35.52759	1:	1.42
B2	B2	B9	B9	0.0026	35.52759	1:	2.07
B2	B2	C2	C2	0.0019	34.54914	1:	2.02
B2	B2	C5	C5	0.0024	34.54914	1:	1.06
B2	B2	C9	C9	0.0028	34.54914	1:	0.86
B2	B2	A9	A9	0.0023	34.54914	1:	0.86
B2	B2	B9	B9	0.0023	34.54914	1:	0.86
B2	B2	C2	C2	0.0023	34.54914	1:	0.86
B2	B2	C5	C5	0.0023	34.54914	1:	0.86
B2	B2	C9	C9	0.0023	34.54914	1:	0.86
B2	B2	A9	A9	0.0021	34.54914	1:	0.86
B2	B2	B9	B9	0.0021	34.54914	1:	0.86
B2	B2	C2	C2	0.0021	34.54914	1:	0.86
B2	B2	C5	C5	0.0021	34.54914	1:	0.86
B2	B2	C9	C9	0.0021	34.54914	1:	0.86
B2	B2	A9	A9	0.0019	34.54914	1:	0.86
B2	B2	B9	B9	0.0019	34.54914	1:	0.86
B2	B2	C2	C2	0.0019	34.54914	1:	0.86
B2	B2	C5	C5	0.0019	34.54914	1:	0.86
B2	B2	C9	C9	0.0019	34.54914	1:	0.86
B5	B5	B5	B5	0.0027	34.54914	1:	3.39
B5	B5	B9	B9	0.0024	34.54914	1:	1.42
B5	B5	C2	C2	0.0026	34.54914	1:	2.07
B5	B5	C5	C5	0.0027	34.54914	1:	1.42
B5	B5	C9	C9	0.0027	34.54914	1:	1.42
B5	B5	A9	A9	0.0019	34.54914	1:	0.96
B5	B5	B9	B9	0.0019	34.54914	1:	0.96
B5	B5	C2	C2	0.0019	34.54914	1:	0.96
B5	B5	C5	C5	0.0019	34.54914	1:	0.96
B5	B5	C9	C9	0.0019	34.54914	1:	0.96
B5	B5	A9	A9	0.0014	34.54914	1:	2.15
B5	B5	B9	B9	0.0014	34.54914	1:	2.15
B5	B5	C2	C2	0.0014	34.54914	1:	2.15
B5	B5	C5	C5	0.0014	34.54914	1:	2.15
B5	B5	C9	C9	0.0014	34.54914	1:	2.15
B9	B9	B9	B9	0.0025	34.54914	1:	1.73
B9	B9	B5	B5	0.0027	34.54914	1:	0.66
B9	B9	C2	C2	0.0027	34.54914	1:	1.70
B9	B9	C5	C5	0.0027	34.54914	1:	1.70
B9	B9	C9	C9	0.0027	34.54914	1:	1.70
B9	B9	A9	A9	0.0019	34.54914	1:	4.96
B9	B9	B9	B9	0.0019	34.54914	1:	4.96
B9	B9	C2	C2	0.0019	34.54914	1:	4.96
B9	B9	C5	C5	0.0019	34.54914	1:	4.96
B9	B9	C9	C9	0.0019	34.54914	1:	4.96
B9	B9	A9	A9	0.0014	34.54914	1:	4.96
B9	B9	B9	B9	0.0014	34.54914	1:	4.96
B9	B9	C2	C2	0.0014	34.54914	1:	4.96
B9	B9	C5	C5	0.0014	34.54914	1:	4.96
B9	B9	C9	C9	0.0014	34.54914	1:	4.96
B9	B9	A9	A9	0.0011	34.54914	1:	4.96
B9	B9	B9	B9	0.0011	34.54914	1:	4.96
B9	B9	C2	C2	0.0011	34.54914	1:	4.96
B9	B9	C5	C5	0.0011	34.54914	1:	4.96
B9	B9	C9	C9	0.0011	34.54914	1:	4.96
B9	B9	A9	A9	0.0011	34.54914	1:	4.96
B9	B9	B9	B9	0.0011	34.54914	1:	4.96
B9	B9	C2	C2	0.0011	34.54914	1:	4.96
B9	B9	C5	C5	0.0011	34.54914	1:	4.96
B9	B9	C9	C9	0.0011	34.54914	1:	4.96
B9	B9	A9	A9	0.0011	34.54914	1:	4.96
B9	B9	B9	B9	0.0011	34.54914	1:	4.96
B9	B9	C2	C2	0.0011	34.54914	1:	4.96
B9	B9	C5	C5	0.0011	34.54914	1:	4.96
B9	B9	C9	C9	0.0011	34.54914	1:	4.96
B9	B9	A9	A9</				